

# Phantom Traffic Jams and Autonomous Vehicles

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*The driver ahead of you brakes, so you brake, which causes braking behind you. But there is no discernable cause. . .*

## Phantom Traffic Jam

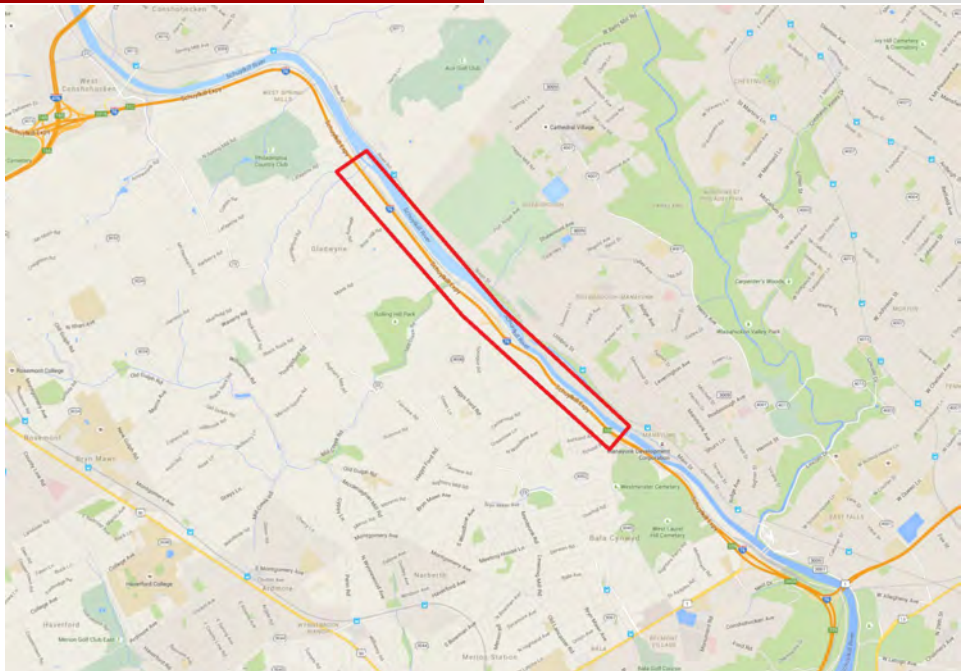
Initially uniform traffic flow of vehicles becomes inhomogeneous, in the absence of obstacles.

## Jamiton

- Traveling wave in traffic flow [c.f. *soliton* = nonlinear wave in physics]
- Vehicles run into a sharp front, break heavily, then slowly speed up.
- Hot-spot for accidents; increased fuel consumption.

## Research Goals

- Understand causes and dynamics of phantom traffic jams.
- Use this knowledge to devise technology to prevent/dissolve them.



## Observation: Jamitons on Long Road (video: [D. Helbing])



## Experiment: Jamitons on Circular Road [Sugiyama et al.: New J. of Physics 2008]



# Traffic Models

## Microscopic: $N$ Vehicles on Road

- Position of  $j$ -th vehicle:  $x_j$
- Velocity of  $j$ -th vehicle:  $v_j$
- Acceleration of  $j$ -th vehicle:  $a_j$

## Physical Principles

- Velocity is rate of change of position:  $v_j = \dot{x}_j$
- Acceleration is rate of change of velocity:  $a_j = \dot{v}_j = \ddot{x}_j$



use computers  
to simulate  $\rightarrow$

## “Follow the Leader” Model

Accelerate/decelerate towards velocity of vehicle ahead of you:

$$a_j = \frac{v_{j+1} - v_j}{x_{j+1} - x_j}$$

## “Optimal Velocity” Model

Accelerate/decelerate towards an optimal velocity that depends on your distance to the vehicle ahead:

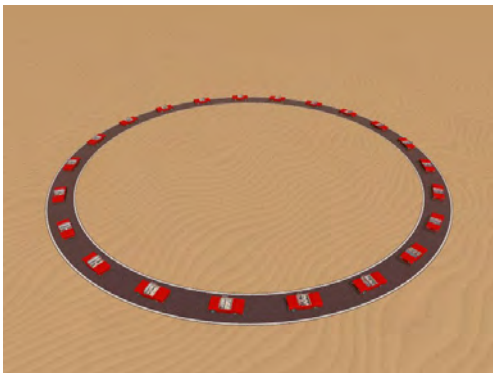
$$a_j = V(x_{j+1} - x_j) - v_j$$

## Combined Model

$$a_j = \alpha \frac{v_{j+1} - v_j}{x_{j+1} - x_j} + \beta (V(x_{j+1} - x_j) - v_j)$$

## Microscopic Traffic Models

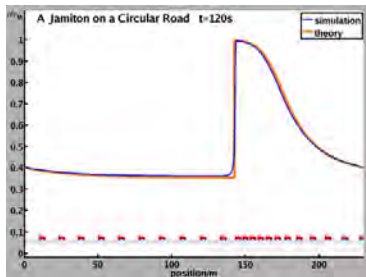
**Simulation:** phantom jams and jamitons



## Macroscopic Traffic Models

$$\begin{cases} \rho_t + (\rho u)_x & = 0 \\ (u+h)_t + u(u+h)_x & = \frac{1}{\tau}(U-u) \end{cases}$$

Describe traffic via fluid dynamics.



- up-scale simulations to large metro areas
- incomplete data and privacy

## Key Point: Instability

- In real traffic there are constant perturbations: road bumps, engine hick-ups, driver inattention, etc.
- These effects are too **small** to produce large-scale phenomena (such as traffic waves) alone.
- Phantom traffic jams arise when uniform traffic flow is **unstable**.
- **Stable traffic flow**: small perturbations of uniform flow decay.
- **Instability**: small perturbations of uniform flow amplify, and eventually grow into large traffic waves (“jamitons”).
- Traffic models reveal: there is a critical threshold density  $\rho_c$  (depending on driver behavior):  
Below  $\rho_c$ , uniform flow is stable; above  $\rho_c$ , unstable.

### Crucial Practical Insight

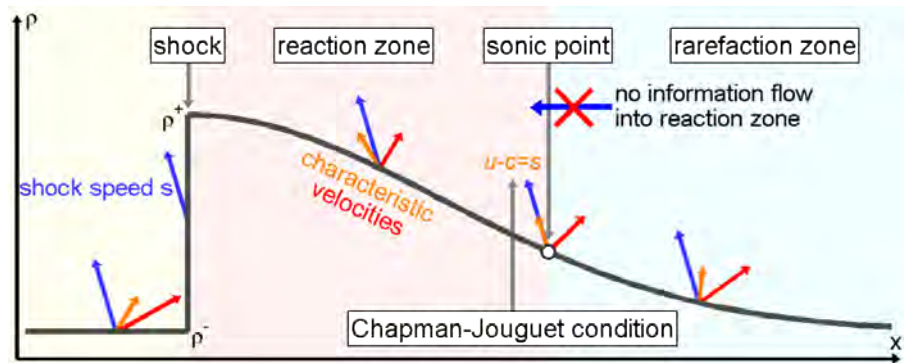
Phantom jams can result from collective driving behavior;  
no bad drivers needed for them to arise.



# Jamitons are mathematical analogs of detonation waves

## Self-Sustained Detonation Wave

Vehicle acceleration plays role of chemical reactions.



Vehicles run into a sharp increase in density ("shock" = braking zone). Attached to shock is a "reaction zone" that ends at a sonic point. Sonic point is event horizon: once passed, a vehicle cannot affect jamiton.

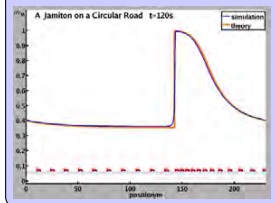
## Founders of Detonation Theory

Chapman  
1899Jouguet  
1905Zel'dovich  
1910von Neumann  
1942Döring  
1943

## Roll waves

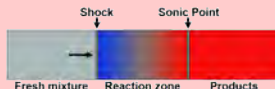


## Traffic wave



## Detonation wave

A shock supported by a trailing exothermic reaction



## Detonations

- combustion
- certain explosions

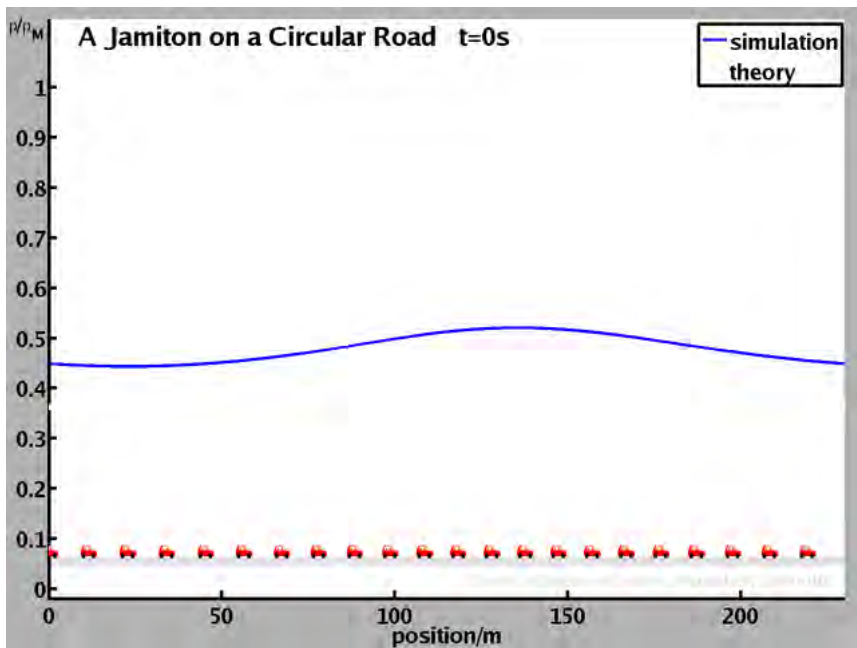
## Black hole

sonic point = event horizon

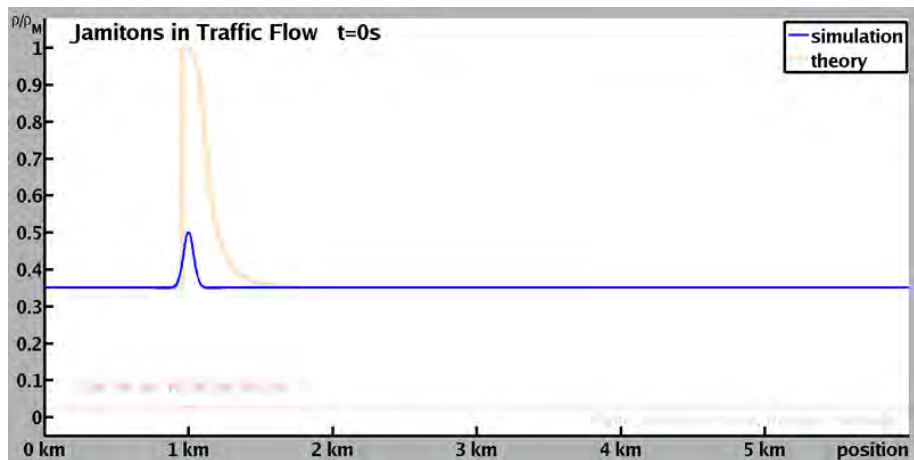


## Hydraulic jump





Infinite road; lead jamiton gives birth to a chain of “jamitinos”.



## Collaborators

Benedetto Piccoli (Rutgers Math)  
Jonathan Sprinkle (U of Arizona ElecEng)  
Daniel Work (UIUC Civil Eng)

## Support

NSF CNS-1446690

*CPS: Synergy: Control of vehicular traffic flow via low density AVs*



- traffic science: understand traffic flow via models, analysis, and computation
- traffic engineering: **develop future traffic control** to prevent/dissolve traffic waves (make whole flow safer and more fuel efficient)
- traditional highway traffic controls: ramp metering, variable speed limits (neither can break up traffic waves)
- **use autonomous vehicles** (AVs); low cost: in 10–15 years, AVs will be on our roads anyways
- human factor in a cyber-physical system: humans interact with AVs; fundamental need to better understand human driving behavior

### Univ. of Arizona AV



## Collaborators

Rodolfo Ruben Rosales (MIT Math)  
Aslan Kasimov (KAUST)  
Morris Flynn (Alberta MechEng)

## Support

NSF DMS-1007899

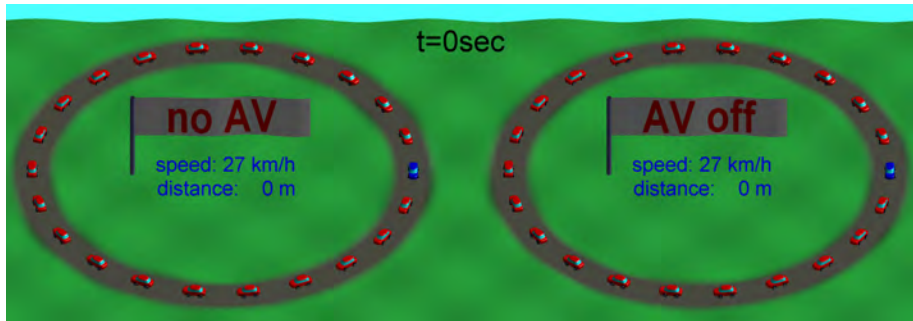
*Phantom traffic jams, continuum modeling, and detonation wave theory*



## Experimental measurements of human driving



## Simulation: uncontrolled vs. AV-controlled traffic flow



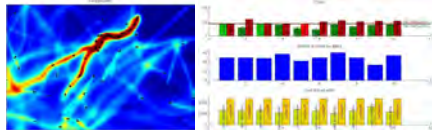
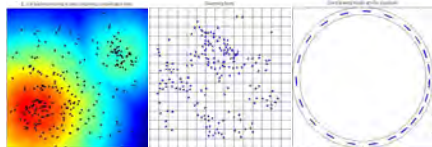
## Media



## Education

New course (Spring 2016):

*CST 2100: Topics in Science and Technology: Modeling and Simulation in Science and Technology*



Without formal programming background, students engage in agent-based modeling and simulation: swarming ants and birds, population dynamics, traffic flow and human crowds, bacterial motion, stock market models, etc.

## Atherosclerotic Plaque Growth

Modeling and simulation of long-term (30 years) growth:

$$\text{LDL \& LDLox: } d_c \Delta c - k_c c M = 0 \quad \text{in } \Omega(t)$$

$$\text{macrophages: } d_M \Delta M - k_M c M = 0 \quad \text{in } \Omega(t)$$

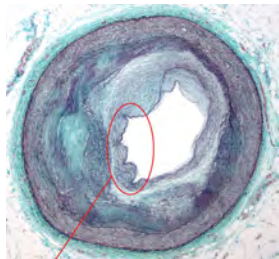
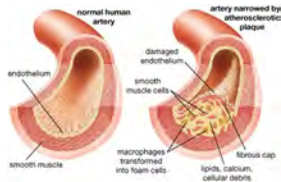
$$\text{foam cells: } F_t + \nabla \cdot (\vec{v} F) = (k_c + k_M) c M \quad \text{in } \Omega(t)$$

$$\text{growth field: } \nabla \cdot \vec{v} = (k_c + k_M) c M \quad \text{in } \Omega(t)$$

$$\text{domain motion: } \dot{\Omega} = \vec{v}$$

### Key Messages

- Research: Ripples observed on plaques can be explained via an instability of the model equations.
- Tiny imperfections grow into wave structures that fundamentally affect the properties of the structure (e.g. risk of rupture) — **same as in traffic waves.**
- **Applied and Computational Mathematics:** model- and equation-driven research; advance mutual insight in seemingly disconnected fields.



Result: ripples can be explained via instability of equations.

### Collaborators

Kurosh Darvish (Temple MechEng)

Pak-Wing Fok (U Delaware)

Sunnie Joshi (Temple University)

### Support

NSF DMS-1318641

*A computational framework for atherosclerotic plaque growth simulations*

